



# Mousehole School Calculation Policy

This policy is intended to detail which calculation strategies are taught in each year group. It was developed to ensure continuity of approach between classes and to act as a supporting document. It is not exhaustive and children are encouraged to select the most accurate and efficient methods depending on the nature of the calculation, the numbers involved and their own learning preference.

This policy has been written in conjunction with the Maths Policy and appears as an appendix to it.



## KEY STAGE 1

Children in Years 1 and 2 will be given a really solid foundation in the basic building blocks of mental and written arithmetic. Through being taught place value, children will develop an understanding of how numbers work, so that they are confident with 2-digit numbers and beginning to read and say numbers above 100.

**Addition and Subtraction:** A focus on number bonds, first via practical hands-on experiences and subsequently using memorisation techniques, enables a good grounding in these crucial facts, and ensures that all children leave Year 2 knowing the pairs of numbers which make all the numbers up to 10 at least. Children will also have experienced and been taught pairs to 20. Children's knowledge of number facts enables them to add several 1-digit numbers, and to add/subtract a 1-digit number to/from a 2-digit number. Another important conceptual tool is the ability to add/subtract 1 or 10, and to understand which digit changes and why. This understanding is extended to enable children to add and subtract multiples of 10 to and from any 2-digit number. The most important application of this knowledge is the ability to add or subtract any pair of 2-digit numbers by counting on or back in 10s and 1s. Children may extend this to adding by partitioning numbers into 10s and 1s.

**Multiplication and Division:** Children will be taught to count in 2s, 3s, 5s and 10s, and will relate this skill to repeated addition. Children will meet and begin to learn the associated  $\times 2$ ,  $\times 3$ ,  $\times 5$  and  $\times 10$  tables. Engaging in a practical way with the concept of repeated addition and the use of arrays enables children to develop a preliminary understanding of multiplication, and asking them to consider how many groups of a given number make a total will introduce them to the idea of division. Children will also be taught to double and halve numbers, and will thus experience scaling up or down as a further aspect of multiplication and division.

**Fractions:** Fractions will be introduced as numbers and as operators, specifically in relation to halves, quarters and thirds.

**Problem solving:**

Solving simple concrete problems

Recognise and create repeating patterns

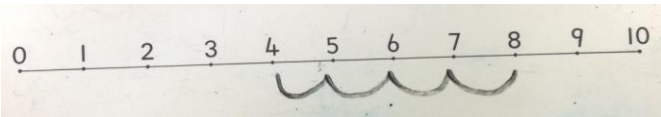
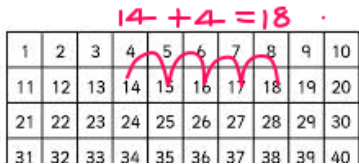
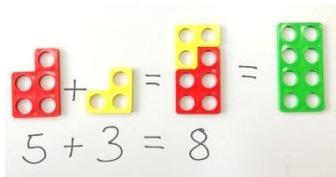
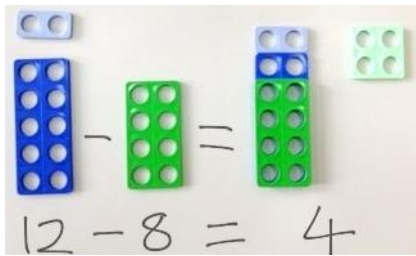
Missing number problems

Addition and subtraction: Solve simple one step problems using concrete objects and pictorial representations

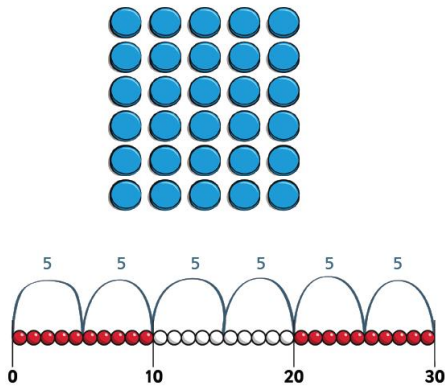
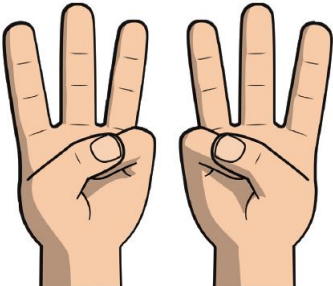
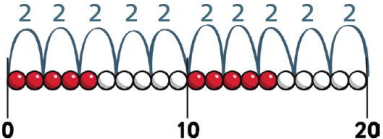
Problems should include the terms: put together, add, altogether, total, take away, distance between, difference between, more than and less than, so that pupils develop the concept of addition and subtraction and are enabled to use these operations flexibly.

Multiplication and division: solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

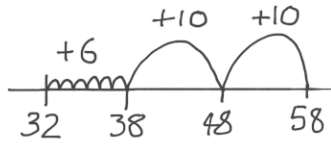
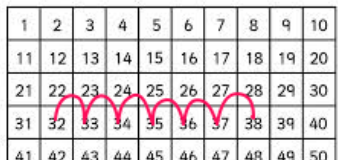
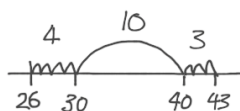
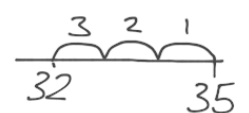
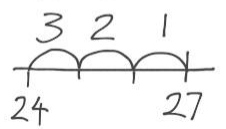


Year 1			
	Mental calculation	Formal calculation	Default for ALL children
Y1 +	<p>Number bonds ('story' of 5, 6, 7, 8, 9 and 10)</p> <p>Count on in 1s from a given 2-digit number</p> <p>Add two 1-digit numbers</p> <p>Add three 1-digit numbers, spotting doubles or pairs to 10</p> <p>Count on in 10s from any given 2-digit number</p> <p>Add 10 to any given 2-digit number</p> <p>Use number facts to add 1-digit numbers to 2-digit numbers e.g. Use <math>4 + 3</math> to work out <math>24 + 3</math>, <math>34 + 3</math></p> <p>Add by putting the larger number first</p>	<p>Using a number track to count on</p>  <p>Use a number square to count on</p>   <p>Counting objects and using Numicon to model calculations</p>	<p>Pairs with a total of 10</p> <p>Count in 1s</p> <p>Count in 10s</p> <p>Count on 1 from any given 2-digit number</p>
Y1 -	<p>Number bonds ('story' of 5, 6, 7, 8, 9 and 10)</p> <p>Count back in 1s from a given 2-digit number</p> <p>Subtract one 1-digit number from another</p> <p>Count back in 10s from any given 2-digit number</p> <p>Subtract 10 from any given 2-digit number</p> <p>Use number facts to subtract 1-digit numbers from 2-digit numbers e.g. Use <math>7 - 2</math> to work out <math>27 - 2</math>, <math>37 - 2</math></p>	<p>Develop inverse understanding alongside adding</p> <p>Using a number track to count back</p> <p>Use a number square to count back</p> <p>Counting objects and using Numicon to model calculations</p>  <p> <math>7 + 6 = 13</math>  so  <math>13 - 6 = 7</math>  and  <math>13 - 7 = 6</math> </p>	<p>Pairs with a total of 10</p> <p>Count back in 1s from 20 to 0</p> <p>Count back in 10s from 100 to 0</p> <p>Count back 1 from any given 2-digit number</p>

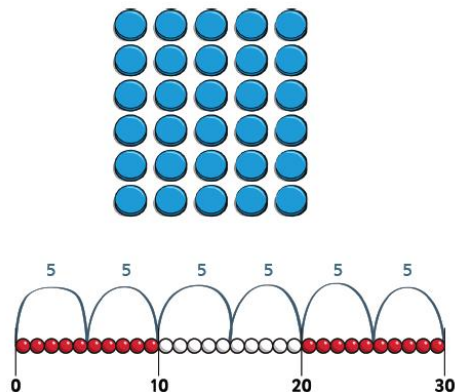
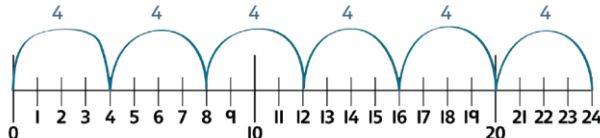


<p><b>Y1</b> <b>×</b></p>	<p>Begin to count in 2s, 5s and 10s Begin to say what three 5s are by counting in 5s, or what four 2s are by counting in 2s, etc. Double numbers to 10</p>	<p>Arrays e.g. <math>6 \times 5</math> as six steps in the 5s count as well as six lots of five</p>  <p>As repeated addition  <math>4 \times 3 = 3 \times 4</math>  <math>= 4 + 4 + 4</math>  <math>= 3 + 3 + 3 + 3</math></p> <p>Doubling and halving</p>	<p>Begin to count in 2s and 10s Double numbers to 5 using fingers</p> 
<p><b>Y1</b> <b>÷</b></p>	<p>Begin to count in 2s, 5s and 10s Find half of even numbers to 12 and know it is hard to halve odd numbers Find half of even numbers by sharing Begin to use visual and concrete arrays or 'sets of' to find how many sets of a small number make a larger number</p>	<p>"Clever" counting (counting in 2s or 5s) Count in 2s</p>  <p>Recognising as inverse of multiplication</p> $3 \times \boxed{?} = 12$ $12 \div 3 = \boxed{?}$	<p>Begin to count in 2s and 10s Find half of even numbers by sharing</p>



Year 2			
	Mental calculation	Written calculation	Default for ALL children
Y2 +	<p>Number bonds – know all the pairs of numbers which make all the numbers to 12, and pairs with a total of 20</p> <p>Count on in 1s and 10s from any given 2-digit number</p> <p>Add two or three 1-digit numbers</p> <p>Add a 1-digit number to any 2-digit number using number facts, including bridging multiples of 10 e.g. <math>45 + 4</math> e.g. <math>38 + 7</math></p> <p>Add 10 and small multiples of 10 to any given 2-digit number</p> <p>Add any pair of 2-digit numbers</p>	<p>Make links between number facts e.g.</p> <p><math>5 + 3 = 8</math> so</p> <p><math>35 + 3 = 38</math></p> <p><math>5 + 63 = 68</math></p> <p>Using number lines to count on (units first then tens)</p> <p><math>32 + 26 = 58</math></p> 	<p>Know pairs of numbers which make each total up to 10</p> <p>Add two 1-digit numbers</p> <p>Add a 1-digit number to a 2-digit number by counting on in 1s</p> <p>Add 10 and small multiples of 10 to a 2-digit number by counting on in 10s</p>
Y2 -	<p>Number bonds – know all the pairs of numbers which make all the numbers to 12</p> <p>Count back in 1s and 10s from any given 2-digit number</p> <p>Subtract a 1-digit number from any 2-digit number using number facts, including bridging multiples of 10 e.g. <math>56 - 3</math> e.g. <math>53 - 5</math></p> <p>Subtract 10 and small multiples of 10 from any given 2-digit number</p> <p>Subtract any pair of 2-digit numbers by counting back in 10s and 1s or by counting up</p>	<p><math>38 - 6 = 32</math></p>  <p>Count back to take away using a number line or square</p> <p><math>43 - 26 = 4 + 10 + 3 = 17</math></p>  <p>Counting in units and then tens</p> <p>"Mind the gap" between the numbers which are close together</p> <p><math>35 - 32 = 3</math></p>  <p>Counting back (robbery)</p> <p>Finding the difference (mind the gap)</p>	<p>Know pairs of numbers which make each total up to 10</p> <p>Subtract a 1-digit number from a 2-digit number by counting back in 1s</p> <p>Subtract 10 and small multiples of 10 from a 2-digit number by counting back in 10s</p> <p>"Robbing" a small number</p> <p><math>27 - 3 = 24</math></p> 



<p><b>Y2</b> <b>×</b></p>	<p>Count in 2s, 5s and 10s Begin to count in 3s Begin to understand that multiplication is repeated addition and to use arrays e.g. <math>3 \times 4</math> is three rows of 4 dots Begin to learn the <math>\times 2</math>, <math>\times 3</math>, <math>\times 5</math> and <math>\times 10</math> tables, seeing these as 'lots of' e.g. 5 lots of 2, 6 lots of 2, 7 lots of 2 Double numbers up to 20 Begin to double multiples of 5 to 100 Begin to double 2-digit numbers less than 50 with 1s digits of 1, 2, 3, 4 or 5</p>	<p>Arrays</p>  <p>Understand that <math>5 \times 3</math> can be worked out as three 5s or five 3s</p> <p>As repeated addition <math>4 \times 3 = 4 + 4 + 4 = 3 + 3 + 3 + 3</math></p> <p>Language of scaling: Lots of ... groups of... n times bigger...</p>	<p>Count in 2s, 5s and 10s Begin to use and understand simple arrays e.g. <math>2 \times 4</math> is two lots of four Double numbers up to 10 double 8 <math>8 = 5 + 3</math> <math>10 + 6 = 16</math> Double multiples of 10 to 50</p>
<p><b>Y2</b> <b>÷</b></p>	<p>Count in 2s, 5s and 10s Begin to count in 3s Using fingers, say where a given number is in the 2s, 5s or 10s count e.g. 8 is the fourth number when I count in 2s Relate division to grouping e.g. How many groups of 5 in 15? Halve numbers to 20 Begin to halve numbers to 40 and multiples of 10 to 100 Find <math>\frac{1}{2}</math>, <math>\frac{1}{3}</math>, <math>\frac{1}{4}</math> and <math>\frac{3}{4}</math> of a quantity of objects and of amounts (whole number answers)</p>	<p>"Clever" counting (counting in 2s or 5s)</p>  <p>"How many groups of five do I count to get to twenty?"</p> <p><math>\boxed{?} \times 5 = 15</math> <math>15 \div 5 = \boxed{?}</math></p> <p>Recognising as inverse of multiplication</p> <p>Begin to recognise <math>\frac{1}{2}</math> and <math>\frac{1}{4}</math> of small quantities</p>	<p>Count in 2s, 5s and 10s Say how many rows in a given array e.g. How many rows of 5 are in an array of <math>3 \times 5</math>? Halve numbers to 12 Find <math>\frac{1}{2}</math> of amounts</p>



## LOWER KEY STAGE 2

In Lower Key Stage 2, children build on the concrete and conceptual understandings they have gained in Key Stage 1 to develop a real mathematical understanding of the four operations, in particular developing arithmetical competence in relation to larger numbers.

**Addition and subtraction:** Children are taught to use place value and number facts to add and subtract numbers mentally and they will develop a range of strategies to enable them to discard the 'counting in 1s' or fingers-based methods of Key Stage 1. In particular, children will learn to add and subtract multiples and near multiples of 10, 100 and 1000, and will become fluent in complementary addition as an accurate means of achieving fast and accurate answers to 3-digit subtractions. Standard written methods for adding larger numbers are taught, learned and consolidated, and written column subtraction is also introduced.

**Multiplication and division:** This key stage is also the period during which all the multiplication and division facts are thoroughly memorised, including all facts up to  $12 \times 12$ . Efficient written methods for multiplying or dividing a 2-digit or 3-digit number by a 1-digit number are taught, as are mental strategies for multiplication or division with large but 'friendly' numbers, e.g. when dividing by 5 or multiplying by 20.

**Fractions and decimals:** Children will develop their understanding of fractions, learning to reduce a fraction to its simplest form, as well as finding non-unit fractions of amounts and quantities. The concept of a decimal number is introduced and children consolidate a firm understanding of 1-place decimals, multiplying and dividing whole numbers by 10 and 100.

### **Solving problems:**

Pupils solve simple problems in contexts, deciding which of the four operations to use and why. These include measuring and scaling contexts, (for example, four times as high, eight times as long etc.) and correspondence problems in which  $m$  objects are connected to  $n$  objects (for example, 3 hats and 4 coats, how many different outfits?; 12 sweets shared equally between 4 children; 4 cakes shared equally between 8 children).

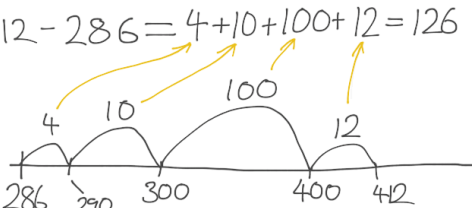
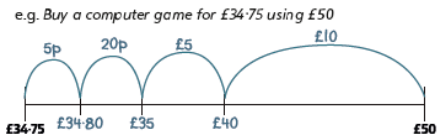
Using a variety of representations to solve problems across the whole maths curriculum and specifically:

- Missing number problems
- One step and two step data handling problems
- Addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why.
- Simple measure and money problems involving fractions and decimals to two decimal places.
- Converting from hours to minutes; minutes to seconds; years to months; weeks to days.





## Year 3

	Mental calculation	Written calculation	Default for ALL children
<b>Y3</b> <b>+</b>	<p>Know pairs with each total to 20 e.g. <math>2 + 6 = 8</math>, <math>12 + 6 = 18</math>, <math>7 + 8 = 15</math></p> <p>Know pairs of multiples of 10 with a total of 100</p> <p>Add any two 2-digit numbers by counting on in 10s and 1s or by using partitioning</p> <p>Add multiples and near multiples of 10 and 100</p> <p>Perform place-value additions without a struggle e.g. <math>300 + 8 + 50 = 358</math></p> <p>Use place value and number facts to add a 1-digit or 2-digit number to a 3-digit number e.g. <math>104 + 56</math> is 160 since <math>104 + 50 = 154</math> and <math>6 + 4 = 10</math> <math>676 + 8</math> is 684 since <math>8 = 4 + 4</math> and <math>76 + 4 + 4 = 84</math></p> <p>Add pairs of 'friendly' 3-digit numbers e.g. <math>320 + 450</math></p> <p>Begin to add amounts of money using partitioning</p>	<p>Use expanded column addition to add two or three 3-digit numbers or three 2-digit numbers</p> <p><i>Expanded column</i>  <math display="block">\begin{array}{r} 324 + 537 = 861 \\ 300 \quad 20 \quad 4 \\ + 500 \quad 30 \quad 7 \\ \hline 800 \quad 60 \quad 1 \\ \hline 10 \end{array}</math></p> <p>Begin to use compact column addition to add numbers with 3 digits</p> <p>Begin to add like fractions e.g. <math>\frac{3}{8} + \frac{1}{8} + \frac{1}{8}</math></p> <p>Recognise fractions that add to 1 e.g. <math>\frac{1}{4} + \frac{3}{4}</math> e.g. <math>\frac{3}{5} + \frac{2}{5}</math></p> <p><i>Compact column</i>  <math display="block">\begin{array}{r} 538 \\ + 624 \\ \hline 1162 \\ \hline 1 \end{array}</math></p>	<p>Know pairs of numbers which make each total up to 10, and which total 20</p> <p>Add two 2-digit numbers by counting on in 10s and 1s e.g. <math>56 + 35</math> is <math>56 + 30</math> and then add the 5</p> <p>Understand simple place-value additions e.g. <math>200 + 40 + 5 = 245</math></p> <p>Use place value to add multiples of 10 or 100</p>
<b>Y3</b> <b>-</b>	<p>Know pairs with each total to 20 e.g. <math>8 - 2 = 6</math> e.g. <math>18 - 6 = 12</math> e.g. <math>15 - 8 = 7</math></p> <p>Subtract any two 2-digit numbers</p> <p>Perform place-value subtractions without a struggle e.g. <math>536 - 30 = 506</math></p> <p>Subtract 2-digit numbers from numbers <math>&gt; 100</math> by counting up</p> <p>Subtract multiples and near multiples of 10 and 100</p> <p>Find change from £1, £5 and £10</p>	<p><math>412 - 286 = 4 + 10 + 100 + 12 = 126</math></p>  <p>Use counting up as an informal written strategy for subtracting pairs of 3-digit numbers</p> <p>e.g. Buy a computer game for £34.75 using £50</p> 	<p>Know pairs of numbers which make each total up to 10, and which total 20</p> <p>Count up to subtract 2-digit numbers e.g. <math>72 - 47</math></p> <p>Subtract multiples of 5 from 100 by counting up e.g. <math>100 - 35</math></p> <p>Subtract multiples of 10 and 100</p>





<p><b>Y3</b> <b>×</b></p>	<p>Know by heart all the multiplication facts in the <math>\times 2</math>, <math>\times 3</math>, <math>\times 4</math>, <math>\times 5</math>, <math>\times 8</math> and <math>\times 10</math> tables          Multiply whole numbers by 10 and 100          Recognise that multiplication is commutative          Use place value and number facts in mental multiplication              e.g. <math>30 \times 5</math> is <math>15 \times 10</math>          Partition teen numbers to multiply by a 1-digit number              e.g. <math>3 \times 14</math> as <math>3 \times 10</math> and <math>3 \times 4</math>          Double numbers up to 50</p>	<p>Use partitioning (grid multiplication) to multiply 2-digit and 3-digit numbers by 'friendly' 1-digit numbers</p> <p>e.g. <math>253 \times 6</math></p> <table border="1" data-bbox="1072 363 1413 467"> <tr> <td><math>\times</math></td><td>200</td><td>50</td><td>3</td></tr> <tr> <td>6</td><td>1200</td><td>300</td><td>18</td></tr> </table> <p>= 1518</p>	$\times$	200	50	3	6	1200	300	18	<p>Know by heart the <math>\times 2</math>, <math>\times 3</math>, <math>\times 5</math> and <math>\times 10</math> tables          Double given tables facts to get others          Double numbers up to 25 and multiples of 5 to 50</p>
$\times$	200	50	3								
6	1200	300	18								
<p><b>Y3</b> <b>÷</b></p>	<p>Know by heart all the division facts derived from the <math>\times 2</math>, <math>\times 3</math>, <math>\times 4</math>, <math>\times 5</math>, <math>\times 8</math> and <math>\times 10</math> tables          Divide whole numbers by 10 or 100 to give whole number answers          Recognise that division is not commutative          Use place value and number facts in mental division              e.g. <math>84 \div 4</math> is half of 42          Divide larger numbers mentally by subtracting the 10th multiple as appropriate, including those with remainders              e.g. <math>57 \div 3</math> is <math>10 + 9</math> as <math>10 \times 3 = 30</math> and <math>9 \times 3 = 27</math>          Halve even numbers to 100, halve odd numbers to 20</p>	<p><math>86 \div 3 = \square</math></p> <p><math>\square \times 3 = 86</math>      <math>86 \div 3 = 28 \text{ r}2</math></p> <p><math>20 \times 3 = 60</math></p> <p><math>26</math></p> <p><math>8 \times 3 = 24</math></p> <p><math>2</math></p> <p><math>28</math></p> <p>Perform divisions just above the 10th multiple using horizontal or vertical jottings and understanding how to give a remainder as a whole number</p> <p>Find unit fractions of quantities and begin to find non-unit fractions of quantities</p>	<p>Know by heart the division facts derived from the <math>\times 2</math>, <math>\times 3</math>, <math>\times 5</math> and <math>\times 10</math> tables          Halve even numbers up to 50 and multiples of 10 to 100          Perform divisions within the tables including those with remainders              e.g. <math>38 \div 5</math></p>								



Year 4			
	Mental calculation	Written calculation	Default for ALL children
Y4 +	<p>Add any two 2-digit numbers by partitioning or counting on</p> <p>Know by heart/quickly derive number bonds to 100 and to £1</p> <p>Add to the next 100, £1 and whole number</p> <p>e.g. <math>234 + 66 = 300</math></p> <p>e.g. <math>3.4 + 0.6 = 4</math></p> <p>Perform place-value additions without a struggle</p> <p>e.g. <math>300 + 8 + 50 + 4000 = 4358</math></p> <p>Add multiples and near multiples of 10, 100 and 1000</p> <p>Use place value and number facts to add 1-, 2-, 3- and 4-digit numbers where a mental calculation is appropriate</p> <p>e.g. <math>4004 + 156 = 4160</math></p>	<p>Column addition for 3-digit and 4-digit numbers</p> <p>e.g. or</p> <p><i>Compact column</i></p> $538 + 624 = 1162$ $\begin{array}{r} 538 \\ + 624 \\ \hline 1162 \end{array}$ <p><i>Expanded column</i></p> $\begin{array}{r} 347 \\ 286 \\ 495 + \\ \hline 1128 \\ 21 \end{array}$ <p>Add like fractions</p> <p>e.g. <math>\frac{3}{5} + \frac{4}{5} = \frac{7}{5} = 1\frac{2}{5}</math></p> <p>Be confident with fractions that add to 1 and fraction complements to 1 e.g. <math>\frac{2}{3} + \_ = 1</math></p>	<p>Add any 2-digit numbers by partitioning or counting on</p> <p>Number bonds to 20</p> <p>Know pairs of multiples of 10 with a total of 100</p> <p>Add 'friendly' larger numbers using knowledge of place value and number facts</p> <p>Use expanded column addition to add 3-digit numbers</p>
Y4 -	<p>Subtract any two 2-digit numbers</p> <p>Know by heart/quickly derive number bonds to 100</p> <p>Perform place-value subtractions without a struggle</p> <p>e.g. <math>4736 - 706 = 4030</math></p> <p>Subtract multiples and near multiples of 10, 100, 1000, £1 and 10p</p> <p>Subtract multiples of 0.1</p> <p>Subtract by counting up</p> <p>e.g. <math>503 - 368</math> is done by adding <math>368 + 2 + 30 + 100 + 3</math> (so we added 135)</p> <p>Subtract, when appropriate, by counting back or taking away, using place value and number facts</p> <p>Subtract £1, 10p, 1p from amounts of money</p> <p>Find change from £10, £20 and £50</p>	<p><i>Expanded column</i></p> $726 - 358 = 368$ $\begin{array}{r} 600 \ 100 \ 16 \\ 700 \ 20 \ 6 \\ - 300 \ 50 \ 8 \\ \hline 300 \ 60 \ 8 \end{array}$ <p>Use expanded column subtraction for 3- and 4-digit numbers</p> <p>Use complementary addition to subtract amounts of money, and for subtractions where the larger number is a near multiple of 1000 or 100</p> <p><math>2002 - 1865 = 35 + 102 = 137</math></p>	<p>Use counting up with confidence to solve most subtractions, including finding complements to multiples of 100</p> <p>e.g. <math>512 - 287</math></p> <p>e.g. <math>67 + \_ = 100</math></p> <p>Use fractions that add to 1 to find fraction complements to 1</p>



<p><b>Y4</b> <b>×</b></p>	<p>Know by heart all the multiplication facts up to <math>12 \times 12</math></p> <p>Recognise factors up to 12 of 2-digit numbers</p> <p>Multiply whole numbers and 1-place decimals by 10, 100, 1000</p> <p>Multiply multiples of 10, 100 and 1000 by 1-digit numbers e.g. <math>300 \times 6</math> e.g. <math>4000 \times 8</math></p> <p>Use understanding of place value and number facts in mental multiplication e.g. <math>36 \times 5</math> is half of <math>36 \times 10</math> e.g. <math>50 \times 60 = 3000</math></p> <p>Partition 2-digit numbers to multiply by a 1-digit number mentally e.g. <math>4 \times 24</math> as <math>4 \times 20</math> and <math>4 \times 4</math></p> <p>Begin to double amounts of money e.g. <math>\pounds 35.60</math> doubled is <math>\pounds 71.20</math></p>	<p>e.g. <math>253 \times 6</math></p> $\begin{array}{r} 253 \\ \times 6 \\ \hline 1200 \leftarrow 6 \times 200 \\ 300 \leftarrow 6 \times 50 \\ + 18 \leftarrow 6 \times 3 \\ \hline 1518 \end{array}$ <p>e.g. <math>16 \times 48</math></p> <table border="1" style="display: inline-table; vertical-align: middle;"> <tr> <td>×</td> <td>10</td> <td>6</td> <td></td> </tr> <tr> <td>40</td> <td>400</td> <td>240</td> <td>= 640</td> </tr> <tr> <td>8</td> <td>80</td> <td>48</td> <td>= 128</td> </tr> <tr> <td></td> <td></td> <td></td> <td><u>768</u></td> </tr> </table> <p>Use a vertical written method to multiply a 1-digit number by a 3-digit number (ladder method)</p> <p>Use an efficient written method to multiply a 2-digit number by a number between 10 and 20 by partitioning (grid method)</p>	×	10	6		40	400	240	= 640	8	80	48	= 128				<u>768</u>	<p>Know by heart multiplication tables up to <math>10 \times 10</math></p> <p>Multiply whole numbers by 10 and 100</p> <p>Use the grid method to multiply a 2-digit or a 3-digit number by a number <math>\leq 6</math></p>
×	10	6																	
40	400	240	= 640																
8	80	48	= 128																
			<u>768</u>																
<p><b>Y4</b> <b>÷</b></p>	<p>Know by heart all the division facts up to <math>144 \div 12</math></p> <p>Divide whole numbers by 10, 100, to give whole number answers or answers with 1 decimal place</p> <p>Divide multiples of 100 by 1-digit numbers using division facts e.g. <math>3200 \div 8 = 400</math></p> <p>Use place value and number facts in mental division e.g. <math>245 \div 20</math> is half of <math>245 \div 10</math></p> <p>Divide larger numbers mentally by subtracting the 10th or 20th multiple as appropriate e.g. <math>156 \div 6</math> is <math>20 + 6</math> as <math>20 \times 6 = 120</math> and <math>6 \times 6 = 36</math></p> <p>Find halves of even numbers to 200 and beyond using partitioning</p> <p>Begin to halve amounts of money e.g. half of <math>\pounds 52.40</math> is <math>\pounds 26.20</math></p>	<p><math>243 \div 8 = \square</math>  <math>\square \times 8 = 243</math>  <math>20 \times 8 = 160</math>  <math>10 \times 8 = 80</math>  <math>30</math>  <math>243 \div 8 = 30 \text{ r } 3</math></p> <p><math>\frac{3}{4}</math> of <math>80 = 60</math>  <math>\frac{1}{7}</math> of <math>42 = 6</math></p> <p>Use a written method to divide a 2-digit or a 3-digit number by a 1-digit number</p> <p>Give remainders as whole numbers</p> <p>Begin to reduce fractions to their simplest forms</p> <p>Find unit and non-unit fractions of larger amounts</p>	<p>Know by heart all the division facts up to <math>100 \div 10</math></p> <p>Divide whole numbers by 10 and 100 to give whole number answers or answers with 1 decimal place</p> <p>Perform divisions just above the 10th multiple using the written layout and understanding how to give a remainder as a whole number</p> <p>Find unit fractions of amounts</p>																



## UPPER KEY STAGE 2

Children move on from dealing mainly with whole numbers to performing arithmetic operations with both decimals and fractions.

**Addition and subtraction:** Children will consolidate their use of written procedures in adding and subtracting whole numbers with up to 6 digits and also decimal numbers with up to 2 decimal places. Mental strategies for adding and subtracting increasingly large numbers will also be taught. These will draw upon children's robust understanding of place value and knowledge of number facts. Negative numbers will be added and subtracted.

**Multiplication and division:** Efficient and flexible strategies for mental multiplication and division are taught and practised, so that children can perform appropriate calculations even when the numbers are large, such as  $40\,000 \times 6$  or  $40\,000 \div 8$ . In addition, it is in Years 5 and 6 that children extend their knowledge and confidence in using written algorithms for multiplication and division.

**Fractions, decimals, percentages and ratio:** Fractions and decimals are also added, subtracted, divided and multiplied, within the bounds of children's understanding of these more complicated numbers. Children will also calculate simple percentages and ratios.

### Problem Solving

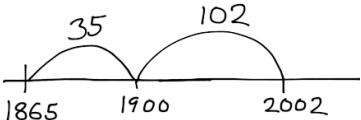
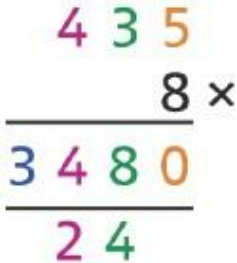
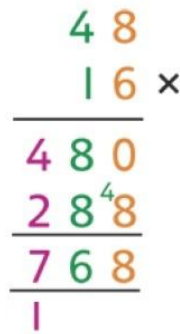
Solve problems involving all four operations specifically:

- multi-step addition and subtraction problems in contexts, deciding which operations and methods to use and why.
- multiplication and division problems including simple fractions and problems involving simple rates and knowledge of factors and multiples, squares and cubes
- addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign
- involving numbers up to three decimal places
- percentage and decimal equivalents of  $\frac{1}{2}$ ,  $\frac{1}{4}$ ,  $\frac{1}{5}$ ,  $\frac{2}{5}$ ,  $\frac{4}{5}$  and those fractions with a denominator of a multiple of 10 or 25
- going beyond the measurement and money models of decimals, for example, by solving puzzles involving decimals.
- solving comparison, sum and difference problems using information presented in a line graph
- complete, read and interpret information in tables, including timetables
- solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison
- involving similar shapes where the scale factor is known or can be found
- measures problems: involving time [converting between units of time], money and measure [for example, length, mass, volume, money] using decimal notation, including scaling and problems which require answers to be rounded to specified degrees of accuracy
- involving unequal quantities, for example, 'for every egg you need three spoonfuls of flour', 'of the class are boys'. These problems are the foundation for later formal approaches to ratio and proportion



Year 5			
	Mental calculation	Written calculation	Default for ALL children
<b>Y5</b> <b>+</b>	<p>Know number bonds to 1 and to the next whole number Add to the next 10 from a decimal number e.g. <math>13.6 + 6.4 = 20</math></p> <p>Add numbers with 2 significant digits only, using mental strategies e.g. <math>3.4 + 4.8</math> e.g. <math>23\ 000 + 47\ 000</math></p> <p>Add 1- or 2-digit multiples of 10, 100, 1000, 10 000 and 100 000 e.g. <math>8000 + 7000</math></p> <p>Add near multiples of 10, 100, 1000, 10 000 and 100 000 to other numbers e.g. <math>82\ 472 + 30\ 004</math></p> <p>Add decimal numbers which are near multiples of 1 or 10, including money e.g. <math>6.34 + 1.99</math></p> <p>Use place value and number facts to add two or more 'friendly' numbers, including money and decimals e.g. <math>3 + 8 + 6 + 4 + 7</math> e.g. <math>0.6 + 0.7 + 0.4</math></p>	<p>Use column addition to add two or three whole numbers with up to 5 digits Use column addition to add any pair of 2-place decimal numbers, including amounts of money</p> $\begin{array}{r} 15.68 \\ 27.86 \\ 43.54 \\ \hline 11. \end{array}$ <p>Begin to add related fractions using equivalences e.g. <math>\frac{1}{2} + \frac{1}{6} = \frac{3}{6} + \frac{1}{6}</math></p> <p>Choose the most efficient method in any given situation</p>	<p>Add numbers with only 2 digits which are not zeros e.g. <math>3.4 + 5.8</math></p> <p>Derive swiftly and without any difficulty number bonds to 100</p> <p>Add 'friendly' large numbers using knowledge of place value and number facts e.g. <math>243 + 406 = 649</math></p> <p>Use expanded column addition to add pairs of 4- and 5-digit numbers</p>
<b>Y5</b> <b>-</b>	<p>Subtract numbers with 2 significant digits only, using mental strategies e.g. <math>6.2 - 4.5</math> e.g. <math>72\ 000 - 47\ 000</math></p> <p>Subtract 1- or 2-digit multiples of 10, 100, 1000, 10 000 and 100 000 e.g. <math>8000 - 3000</math> e.g. <math>60\ 000 - 200\ 000</math></p> <p>Subtract 1- or 2-digit near multiples of 10, 100, 1000, 10 000 and 100 000 from other numbers e.g. <math>82\ 472 - 30\ 004</math></p> <p>Subtract decimal numbers which are near multiples of 1 or 10, including money</p>	<p>Choose the most efficient method in any given situation</p> <p>Use compact or expanded column subtraction to subtract numbers with up to 5 digits</p> $\begin{array}{r} 2\ 14\ 7\ 15 \\ \cancel{3}\ \cancel{4}\ 6\ \cancel{8}\ \cancel{5} \\ \hline 1\ 6\ 4\ 5\ 8 \\ 1\ 8\ 2\ 2\ 7 \end{array} -$ <p>Use complementary addition for subtractions of decimal numbers with up to 2 places, including amounts of money</p>	<p>Derive swiftly and without difficulty number bonds to 100</p> <p>Use counting up with confidence to solve most subtractions, including finding complements to multiples of 1000 e.g. <math>3000 - 2387</math></p>



	<p>e.g. <math>6.34 - 1.99</math> e.g. <math>£34.59 - £19.95</math></p> <p>Use counting up subtraction, with knowledge of number bonds to 10, 100 or £1, as a strategy to perform mental subtraction</p> <p>e.g. <math>£10 - £3.45</math> e.g. <math>1000 - 782</math></p> <p>Recognise fraction complements to 1 and to the next whole number</p> <p>e.g. <math>1\frac{2}{5} + \frac{3}{5} = 2</math></p>	<p>Begin to subtract related fractions using equivalences</p> <p>e.g. <math>\frac{1}{2} - \frac{1}{6} = \frac{2}{6}</math></p> <p>Use complementary addition for subtractions where the larger number is a multiple or near</p> <p><math>2002 - 1865 = 35 + 102 = 137</math></p> 	
<p><b>Y5</b> <b>×</b></p>	<p>Know by heart all the multiplication facts up to <math>12 \times 12</math></p> <p>Multiply whole numbers and 1- and 2-place decimals by 10, 100, 1000, 10 000</p> <p>Use knowledge of factors and multiples in multiplication</p> <p>e.g. <math>43 \times 6</math> is double <math>43 \times 3</math> e.g. <math>28 \times 50</math> is <math>\frac{1}{2}</math> of <math>28 \times 100 = 1400</math></p> <p>Use knowledge of place value and rounding in mental multiplication</p> <p>e.g. <math>67 \times 199</math> as <math>67 \times 200 - 67</math></p> <p>Use doubling and halving as a strategy in mental multiplication</p> <p>e.g. <math>58 \times 5</math> is half of <math>58 \times 10</math> e.g. <math>34 \times 4</math> is 34 doubled twice</p> <p>Partition 2-digit numbers, including decimals, to multiply by a 1-digit number mentally</p> <p>e.g. <math>6 \times 27</math> as <math>6 \times 20</math> (120) plus <math>6 \times 7</math> (42) e.g. <math>6.3 \times 7</math> as <math>6 \times 7</math> (42) plus <math>0.3 \times 7</math> (2.1)</p> <p>Double amounts of money by partitioning</p> <p>e.g. <math>£37.45</math> doubled is <math>£37</math> doubled (£74) plus 45p doubled (90p) giving a total of £74.90</p>	<p>Use short multiplication to multiply a 1-digit number by a number with up to 4 digits</p>  <p>Use long multiplication to multiply 3-digit and 4-digit numbers by a number between 11 and 20</p> <p>Choose the most efficient method in any given situation</p> <p>Find simple percentages of amounts</p> <p>e.g. 10%, 5%, 20%, 15% and 50%</p> <p>Begin to multiply fractions and mixed numbers by whole numbers <math>\leq 10</math></p> <p>e.g. <math>4 \times \frac{2}{3} = \frac{8}{3} = 2\frac{2}{3}</math></p> 	<p>Know multiplication tables to <math>11 \times 11</math></p> <p>Multiply whole numbers and 1-place decimals by 10, 100 and 1000</p> <p>Use knowledge of factors as aids to mental multiplication</p> <p>e.g. <math>13 \times 6</math> is double <math>13 \times 3</math> e.g. <math>23 \times 5</math> is <math>\frac{1}{2}</math> of <math>23 \times 10</math></p> <p>Use the grid method to multiply numbers with up to 4 digits by 1-digit numbers</p> <p>Use the grid method to multiply 2-digit numbers by 2-digit numbers</p>



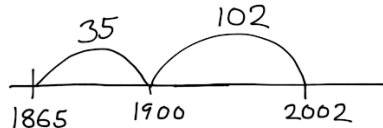
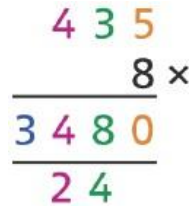
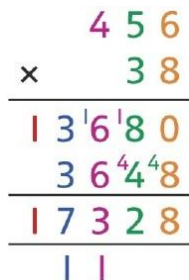
<p><b>Y5</b> <b>÷</b></p>	<p>Know by heart all the division facts up to <math>144 \div 12</math></p> <p>Divide whole numbers by 10, 100, 1000, 10 000 to give whole number answers or answers with 1, 2 or 3 decimal places</p> <p>Use doubling and halving as mental division strategies e.g. <math>34 \div 5</math> is <math>(34 \div 10) \times 2</math></p> <p>Use knowledge of multiples and factors, as well as tests for divisibility, in mental division e.g. <math>246 \div 6</math> is <math>123 \div 3</math> e.g. <i>We know that 525 divides by 25 and by 3</i></p> <p>Halve amounts of money by partitioning e.g. <math>\frac{1}{2}</math> of <math>\pounds 75.40 = \frac{1}{2}</math> of <math>\pounds 75</math> (<math>\pounds 37.50</math>) plus half of 40p (20p) which is <math>\pounds 37.70</math></p> <p>Divide larger numbers mentally by subtracting the 10th or 100th multiple as appropriate e.g. <math>96 \div 6</math> is <math>10 + 6</math>, as <math>10 \times 6 = 60</math> and <math>6 \times 6 = 36</math> e.g. <math>312 \div 3</math> is <math>100 + 4</math> as <math>100 \times 3 = 300</math> and <math>4 \times 3 = 12</math></p> <p>Know tests for divisibility by 2, 3, 4, 5, 6, 9 and 25</p> <p>Know square numbers and cube numbers</p> <p>Reduce fractions to their simplest form</p>	<p>Use short division to divide a number with up to 4 digits by a number <math>\leq 12</math></p> <div style="text-align: right;"> <math display="block">\begin{array}{r} 4 \ 6 \ r \ 1 \\ 3 \overline{) 139} \end{array}</math> </div> <p>Give remainders as whole numbers or as fractions</p> <p>Find non-unit fractions of large amounts</p> <p>Turn improper fractions into mixed numbers and vice versa</p> <div style="text-align: right;"> <math display="block">\frac{7}{3} = 2\frac{1}{3}</math> <math display="block">4\frac{1}{4} = \frac{17}{4}</math> </div> <p>Choose the most efficient method in any given situation</p>	<p>Know by heart division facts up to <math>121 \div 11</math></p> <p>Divide whole numbers by 10, 100 or 1000 to give answers with up to 1 decimal place</p> <p>Use doubling and halving as mental division strategies</p> <p>Use an efficient written method to divide numbers <math>\leq 1000</math> by 1-digit numbers</p> <p>Find unit fractions of 2- and 3-digit numbers</p>
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Year 6			
	Mental calculation	Written calculation	Default for ALL children
Y6 +	<p>Know by heart number bonds to 100 and use these to derive related facts e.g. <math>3.46 + 0.54</math></p> <p>Derive, quickly and without difficulty, number bonds to 1000</p> <p>Add small and large whole numbers where the use of place value or number facts makes the calculation do-able mentally e.g. <math>34\ 000 + 8000</math></p> <p>Add multiples of powers of 10 and near multiples of the same e.g. <math>6345 + 199</math></p> <p>Add negative numbers in a context such as temperature where the numbers make sense</p> <p>Add two 1-place decimal numbers or two 2-place decimal numbers less than 1 e.g. <math>4.5 + 6.3</math> e.g. <math>0.74 + 0.33</math></p> <p>Add positive numbers to negative numbers e.g. <i>Calculate a rise in temperature or continue a sequence beginning with a negative number</i></p>	<p>Use column addition to add numbers with up to 5 digits</p> $\begin{array}{r} \pounds 14.64 \\ \pounds 28.78 \\ \pounds 12.26 + \\ \hline \pounds 55.68 \\ 11.1 \end{array}$ <p>Use column addition to add decimal numbers with up to 3 decimal places</p> <p>Add mixed numbers and fractions with different denominators</p>	<p>Derive, swiftly and without difficulty, number bonds to 100</p> <p>Use place value and number facts to add 'friendly' large or decimal numbers e.g. <math>3.4 + 6.6</math> e.g. <math>26\ 000 + 54\ 000</math></p> <p>Use column addition to add numbers with up to 4-digits</p> <p>Use column addition to add pairs of 2-place decimal numbers</p> $\begin{array}{r} 15.68 \\ 27.86 + \\ \hline 43.54 \\ 11.1 \end{array}$
Y6 -	<p>Use number bonds to 100 to perform mental subtraction of any pair of integers by complementary addition e.g. <math>1000 - 654</math> as <math>46 + 300</math> in our heads</p> <p>Use number bonds to 1 and 10 to perform mental subtraction of any pair of 1-place or 2-place decimal numbers using complementary addition and including money e.g. <math>10 - 3.65</math> as <math>0.35 + 6</math> e.g. <math>\pounds 50 - \pounds 34.29</math> as <math>71p + \pounds 15</math></p> <p>Use number facts and place value to perform mental</p>	<p>Use column subtraction to subtract numbers with up to 6 digits</p> $\begin{array}{r} 2\ 14\ \quad 7\ 15 \\ \cancel{3}\ \cancel{4}\ 6\ \cancel{8}\ \cancel{5} \\ \hline 1\ 6\ 4\ 5\ 8 - \\ \hline 1\ 8\ 2\ 2\ 7 \end{array}$	<p>Use number bonds to 100 to perform mental subtraction of numbers up to 1000 by complementary addition e.g. <math>1000 - 654</math> as <math>46 + 300</math> in our heads</p> <p>Use complementary addition for subtraction of integers up to 10 000 e.g. <math>2504 - 1878</math></p> <p>Use complementary addition for subtractions of 1-place decimal numbers and amounts of money</p>



	<p>subtraction of large numbers or decimal numbers with up to 2 places e.g. <math>467\,900 - 3005</math> e.g. <math>4.63 - 1.02</math></p> <p>Subtract multiples of powers of 10 and near multiples of the same</p> <p>Subtract negative numbers in a context such as temperature where the numbers make sense</p>	<p>Use complementary addition for subtractions where the larger number is a multiple or near multiple of 1000 or 10 000 <math>2002 - 1865 = 35 + 102 = 137</math></p>  <p>Use complementary addition for subtractions of decimal numbers with up to 3 places, including money</p> <p>Subtract mixed numbers and fractions with different denominators</p>	<p>e.g. <math>£7.30 - £3.55</math></p>
<p><b>Y6</b> <b>×</b></p>	<p>Know by heart all the multiplication facts up to <math>12 \times 12</math></p> <p>Multiply whole numbers and decimals with up to 3 places by 10, 100 or 1000 e.g. <math>234 \times 1000 = 234\,000</math></p> <p>Identify common factors, common multiples and prime numbers and use factors in mental multiplication e.g. <math>326 \times 6</math> is <math>652 \times 3</math> which is 1956</p> <p>Use place value and number facts in mental multiplication e.g. <math>4000 \times 6 = 24\,000</math> e.g. <math>0.03 \times 6 = 0.18</math></p> <p>Use doubling and halving as mental multiplication strategies, including to multiply by 2, 4, 8, 5, 20, 50 and 25 e.g. <math>28 \times 25</math> is a quarter of <math>28 \times 100 = 700</math></p> <p>Use rounding in mental multiplication e.g. <math>34 \times 19</math> as <math>(34 \times 20) - 34</math></p> <p>Multiply 1- and 2-place decimals by numbers up to and including 10 using place value and partitioning e.g. <math>3.6 \times 4</math> is <math>12 + 2.4</math> e.g. <math>2.53 \times 3</math> is <math>6 + 1.5 + 0.09</math></p> <p>Double decimal numbers with up to 2 places using partitioning e.g. <math>36.73</math> doubled is double 36 (72) plus double 0.73 (1.46)</p>	<p>Use short multiplication to multiply a 1-digit number by a number with up to 4 digits</p>  <p>Use short multiplication to multiply a 1-digit number by a number with 1 or 2 decimal places, including amounts of money</p> <p>Use long multiplication to multiply a 2-digit number by a number with up to 4 digits</p>  <p>Multiply fractions and mixed numbers by whole numbers</p> <p>Multiply fractions by proper fractions</p> <p>Use percentages for comparison and calculate simple percentages</p>	<p>Know by heart all the multiplication facts up to <math>12 \times 12</math></p> <p>Multiply whole numbers and 1- and 2-place decimals by 10, 100 and 1000</p> <p>Use an efficient written method to multiply a 1-digit or a teen number by a number with up to 4 digits by partitioning (grid method)</p> <p>Multiply a 1-place decimal number up to 10 by a number <math>\leq 100</math> using the grid method</p>



<p><b>Y6</b> <b>÷</b></p>	<p>Know by heart all the division facts up to <math>144 \div 12</math></p> <p>Divide whole numbers by powers of 10 to give whole number answers or answers with up to 3 decimal places</p> <p>Identify common factors, common multiples and primes numbers and use factors in mental division e.g. <math>438 \div 6</math> is <math>219 \div 3</math> which is 73</p> <p>Use tests for divisibility to aid mental calculation</p> <p>Use doubling and halving as mental division strategies, for example to divide by 2, 4, 8, 5, 20 and 25 e.g. <math>628 \div 8</math> is halved three times: 314, 157, 78.5</p> <p>Divide 1- and 2-place decimals by numbers up to and including 10 using place value e.g. <math>2.4 \div 6 = 0.4</math> e.g. <math>0.65 \div 5 = 0.13</math> e.g. <math>\pounds 6.33 \div 3 = \pounds 2.11</math></p> <p>Halve decimal numbers with up to 2 places using partitioning e.g. Half of 36.86 is half of 36 (18) plus half of 0.86 (0.43)</p> <p>Know and use equivalence between simple fractions, decimals and percentages, including in different contexts</p> <p>Recognise a given ratio and reduce a given ratio to its lowest terms</p>	<p>Use short division to divide a number with up to 4 digits by a 1-digit or a 2-digit number</p> $\begin{array}{r} 46 \text{ r } 1 \\ 3 \overline{) 139} \end{array}$ <p>Use long division to divide 3-digit and 4-digit numbers by 'friendly' 2-digit numbers e.g. <math>4176 \div 13</math></p> $\begin{array}{r} 300 + 20 + 1, \text{ r } 3 \\ 13 \overline{) 4176} \\ \underline{-3900} \phantom{00} \\ 276 \\ \underline{-260} \phantom{00} \\ 16 \\ \underline{-13} \phantom{00} \\ 3 \end{array}$ <p>4176 <math>\div</math> 13 = 321 r 3</p> <p>Give remainders as whole numbers or as fractions or as decimals</p> <p>Divide a 1-place or a 2-place decimal number by a number <math>\leq 12</math> using multiples of the divisors</p> <p>Divide proper fractions by whole numbers</p>	<p>Know by heart all the division facts up to <math>144 \div 12</math></p> <p>Divide whole numbers by 10, 100, 1000 to give whole number answers or answers with up to 2 decimal places</p> <p>Use an efficient written method, involving subtracting powers of 10 times the divisor, to divide any number of up to 1000 by a number <math>\leq 12</math> e.g. <math>836 \div 11</math> as <math>836 - 770</math> (<math>70 \times 11</math>) leaving 66 which is <math>6 \times 11</math>, giving the answer 76</p> <p>Divide a 1-place decimal by a number <math>\leq 10</math> using place value and knowledge of division facts</p>
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